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$$-\frac{b}{a} = 1 \rightarrow b = 2a \rightarrow am^2 + 2am + c = 9$$

$$(-1, 9) \rightarrow a - 2a + c = 9 \rightarrow (1, 1) \rightarrow a + 2a + c = 9$$

①

$$\rightarrow a - 2a + c = 9 \rightarrow -a + c = 9 \rightarrow -1 + c = 9 \rightarrow c = 10$$

$$\rightarrow -a + c = 9 \rightarrow c = \frac{10}{1} = 10 \rightarrow y = -\frac{1}{2}x^2 - x + 10$$

$$\Delta > 0 \rightarrow m^2 - 4(m+9) > 0 \rightarrow (m-12)(m+6) > 0 \rightarrow \frac{+}{-} \frac{+}{-} \frac{+}{+} \rightarrow (-\infty, -6) \cup (12, \infty)$$

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$$s > 0 \rightarrow -\frac{m}{2} > 0 \rightarrow m < 0, p > 0 \rightarrow \frac{m+9}{2} > 0 \rightarrow m+9 > 0 \rightarrow m > -9$$

$$\rightarrow m \in (-9, 0)$$

$$-\frac{b}{a} = \frac{1}{2} \rightarrow -\frac{b}{a} = \frac{a}{c} \rightarrow a^2 = -bc \rightarrow 9 = (-2m+1)(1-m)$$

②

$$\rightarrow 9 = -2m + 2m^2 + 1 - m = 2m^2 - 3m - 8 \rightarrow 2m^2 - 3m - 11 = 0$$

$$m^2 - 3m - 11 = 0 \rightarrow (m-11)(m+2) = 0 \rightarrow m = 11, m = -2$$

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$$\Delta > 0 \rightarrow (m = -1 \rightarrow 2m^2 - 3m + 1 = 0 \rightarrow \Delta = 9 - (1 \times 2 \times 1) = 9 - 2 = 7 < 0 \text{ X})$$

$$m = 11/2 \rightarrow 2m^2 - 3m + 1 = 0 \rightarrow \Delta = 9 - (2 \times 11 \times 1) = 9 - 22 = -13 < 0 \text{ X}$$

$$n_1 + n_2 = 1, n_1 n_2 = -1$$

③

$$\rightarrow s' = 4s + \frac{1}{n_1} + n_2 + \frac{1}{n_1} = (s^2 - 5sp) + \frac{n_1 + n_2}{n_1 n_2} = (1^2 + 12) \frac{1}{1} = \frac{13}{1}$$

$$\rightarrow p' = (n_1^2 + \frac{1}{n_1})(n_2^2 + \frac{1}{n_2}) = (n_1 n_2)^2 + \frac{n_1^2 + n_2^2}{n_1 n_2} + \frac{1}{n_1 n_2} = (-1)^2 + \frac{1^2 + 12^2}{-1} + \frac{1}{-1} = 1 - 145 - 1 = -145$$

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$$(n')^2 = \frac{13}{1} - \frac{145}{1} = -132$$

P.P.A

④

$$\left(\sqrt{n^2} + \frac{1}{\sqrt{n^2}} + 1\right) (\sqrt{n^2} - 1) = \sqrt{n^2} \times \sqrt{n^2} (\sqrt{n^2} + 1) (\sqrt{n^2} - 1)$$

$$= n^2 - \sqrt{n^2} + \sqrt{n^2} - 1 + \sqrt{n^2} - \sqrt{n^2} = n^2 - 1 = 2n \rightarrow n^2 - 2n - 1 = 0$$

$$\rightarrow S = n_1 + n_2 = 2$$

④

$$n^2 - 2n - 1 = 0 \quad n_1 = 2, n_2 = -1$$

⑤

$$S = 2n_1 + n_2 = 5n_2 = \frac{5a}{2} \rightarrow 10n_2 = a \rightarrow \frac{5}{2} \pm \frac{5}{2} = \pm 1 = 2$$

$$P = 2n_1 \times n_2 = 2n_1^2 = \frac{5}{2} \rightarrow 9n_1^2 = 5 \rightarrow 2n_1 = \pm 2 \rightarrow n_1 = \pm \frac{2}{2}$$

$$1 - (-1) = 2$$

$$a > 0, \quad \frac{1}{a} > 0, \quad + \frac{1}{a} = \frac{1}{a} \rightarrow S > 0$$

⑥

$$\frac{-b}{a} = \frac{-2 \times a}{a} > 0 \rightarrow -2 - 2a = 0 \rightarrow -2 = 2a \rightarrow a = -\frac{2}{2}$$

$$\left. \begin{array}{l} a = 0 \\ a = -\frac{2}{2} \end{array} \right\} \frac{-\frac{2}{2} \pm 0}{-0 + \frac{2}{2}} = 10$$

$$\rightarrow -\frac{2}{2} < a < 0 \rightarrow \left(-\frac{2}{2} > 0\right) \cap (0, +\infty) = \emptyset \rightarrow \text{no solution}$$

$$\left. \begin{array}{l} y = n^2 + an - 2 \xrightarrow{a} n = -\frac{a}{2} \\ y = -n^2 - 2n + b \xrightarrow{a} n = -1 \end{array} \right\} -\frac{1}{2} = -1 \rightarrow -a = -2 \rightarrow a = 2$$

⑦

$$(1, 1), (2, 1) \rightarrow s^2 + 2s - 2 = 1 \rightarrow s^2 + 2s - 3 = 0 \rightarrow (s+3)(s-1) = 0 \rightarrow s = -3, 1$$

$$\left. \begin{array}{l} s = -3 \rightarrow (-3, 1) \rightarrow \frac{-3 - 3}{-3 + 3} + b = 1 \rightarrow b = 4 \\ s = 1 \rightarrow (1, 1) \rightarrow \frac{-1 - 1}{-1 + 1} + b = 1 \rightarrow b = 4 \end{array} \right\} a \times b = 3 \times 4 = 12$$

⑧

$$\textcircled{1} \quad r n^r - a n + b = 0 \rightarrow S = \frac{a}{r} \quad ; \quad P = \frac{b}{r}$$

⑨ 1

$$\textcircled{2} \quad r a n^r + a n - 4 = 0 \rightarrow S = \frac{-4}{r} = -\frac{1}{r} \quad ;$$

$$S_1 = S_2 + 1 \rightarrow \frac{a}{r} = -\frac{1}{r} + 1 \Rightarrow \frac{1}{r} \rightarrow a = 1$$

$$\textcircled{1} \rightarrow r n^r - n + b = 0 \quad , \quad \textcircled{2} \rightarrow r n^r + n - 4 = 0 \rightarrow r n^r + n - 1 = 0 \rightarrow (n+1)(n-1) = 0$$

$$\rightarrow n_1 = -\frac{1}{r} = -1, \quad n_2 = \frac{1}{r} \rightarrow n_1 n_2 = -\frac{1}{r^2} = -1$$

$$\rightarrow -1 = \frac{b}{r} \rightarrow b = -r$$

$$\rightarrow \left[\frac{ab}{r} \right] = \left[\frac{-4 \times 1}{r} \right] = \left[\frac{-4}{r} \right] = \left[\frac{-1}{r} \right] = \boxed{-1}$$

$$x = \frac{1}{r} \quad ; \quad \rightarrow x^r + 7x + m = 0$$

$$x^r + r x - r m = 0$$

$$\rightarrow x^r - x^r + 7x - r x + m + r m = 0$$

⑩

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$$\rightarrow x = -m \rightarrow x = -m \rightarrow -x = m \rightarrow x^r + 7x + m = 0 \rightarrow x^r + 7x - x = 0$$

$$\rightarrow x^r + 6x = 0 \rightarrow x = 0 \quad ;$$

$$x = -6 \rightarrow m = 6 \quad ;$$

$$\rightarrow n^r + 7m + 6 = (n+6)(n+1) = 0$$

$$\rightarrow n^r + 7n - 6 = (n+6)(n-1) = 0$$

$$\rightarrow -1, 6 \quad ; \quad \rightarrow \left[\frac{ab}{r} \right] = \frac{r - (-1)}{r} = \frac{r+1}{r} = \boxed{\frac{r+1}{r}}$$

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