

المعلم د. م. A

علاء سعاد - Li

(1)

$$\frac{11\pi}{\pi} \times \frac{1\pi}{\pi} = 19\omega - 2\phi_0 = 12\omega \quad \tan 120^\circ = -1$$

$$\frac{10\pi}{\pi} \times \frac{1\pi}{\pi} = 9\omega - 2\phi_0 = 2\omega \quad \sin 120^\circ = \frac{\sqrt{3}}{2}$$

$$\frac{12\pi}{\pi} \times \frac{1\pi}{\pi} = \omega - 2\phi_0 = 2\omega \quad \cos 120^\circ = -\frac{1}{2}$$

$$\text{أيضاً, } -1 \cdot \left(-\frac{\sqrt{3}}{2} \times -\frac{\sqrt{3}}{2} \right) = -\frac{1}{2}$$

$$\text{أيضاً, } \frac{1\sqrt{2}}{2} \times \frac{1\pi}{\pi} = \omega - 2\phi_0 = 1\omega \quad \tan 150^\circ = -\frac{1}{\sqrt{3}}$$

$$\frac{11\pi}{\pi} \times \frac{1\pi}{\pi} = 9\phi_0 - 2\phi_0 = 7\phi_0 \quad \sin 150^\circ = \frac{1}{2}$$

$$\frac{10\pi}{\pi} \times \frac{1\pi}{\pi} = \phi_0 - 2\phi_0 = -\phi_0 \quad \cos 150^\circ = -\frac{\sqrt{3}}{2} \quad \left(-\frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \right) - \frac{1}{2} = -\frac{1}{2} - \frac{1}{2} = -1$$

$$\frac{\cos x - \sin x}{\cos x + \sin x} \div \frac{\sin x}{\sin x} = \frac{\cos x - \sin x}{\frac{\cos x}{\sin x} + \frac{\sin x}{\sin x}} = \frac{\cos x - \sin x}{\cot x + 1} = \frac{12 - 1}{12 + 1} = \frac{11}{13}$$

(2)

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = 2 \quad \cos^2 \alpha = \frac{1}{1 + \tan^2 \alpha} = \frac{1}{1 + 4} = \frac{1}{5} \quad \cos \alpha = -\frac{\sqrt{5}}{5}$$

(3)

$$\text{أيضاً, } \sin^2 \alpha + \cos^2 \alpha = 1 \rightarrow \cos^2 \alpha = 1 - \sin^2 \alpha \rightarrow \cos^2 \alpha = 1 - \frac{4}{5} = \frac{1}{5} \rightarrow \cos \alpha = \pm \frac{1}{\sqrt{5}} = \pm \frac{\sqrt{5}}{5}$$

(4)

$$\cos \alpha = -\frac{\sqrt{5}}{5} \rightarrow \cos \frac{11\pi}{6} = -\frac{\sqrt{3}}{2} \rightarrow \cos \left(\frac{11\pi}{6} + \alpha \right) = \left(-\frac{\sqrt{3}}{2} \right) \left(-\frac{\sqrt{5}}{5} \right) - \left(\frac{1}{2} \right) \left(\frac{\sqrt{5}}{5} \right) = \frac{\sqrt{15}}{10} - \frac{\sqrt{5}}{10} = \frac{\sqrt{5}}{10} (\sqrt{3} - 1)$$

$$\sin(a+b) = \sin a \cos b + \sin b \cos a$$

$$1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha} \rightarrow 1 + \frac{1}{4} = \frac{5}{4} = \frac{1}{\cos^2 \alpha} \rightarrow \cos^2 \alpha = \frac{4}{5} \rightarrow \cos \alpha = \pm \frac{2}{\sqrt{5}}$$

$$\sin^2 \alpha = 1 - \cos^2 \alpha = 1 - \frac{4}{5} = \frac{1}{5} \rightarrow \sin \alpha = \pm \frac{1}{\sqrt{5}} = \pm \frac{\sqrt{5}}{5}$$

$$\sin \left(\frac{11\pi}{6} + \alpha \right) = \left(-\frac{\sqrt{3}}{2} \right) \left(\frac{\sqrt{5}}{5} \right) + \left(\frac{1}{2} \right) \left(-\frac{\sqrt{5}}{5} \right) = -\frac{\sqrt{15}}{10} - \frac{\sqrt{5}}{10} = -\frac{\sqrt{5}}{10} (\sqrt{3} + 1)$$

$$r \sin^2 \alpha + \cos^2 \alpha = \frac{r}{r}$$

$$\cos^2 \alpha = -\frac{r}{r}$$

$$\sin^2 \alpha = 1 - \cos^2 \alpha \rightarrow r(1 - \cos^2 \alpha) + \cos^2 \alpha = \frac{r}{r} \rightarrow -\cos^2 \alpha + r = \frac{r}{r} \rightarrow$$

$$\cos^2 \alpha = \frac{r}{r}, \sin^2 \alpha = 1 - \cos^2 \alpha = 1 - \frac{r}{r} = \frac{1}{r} \quad \tan^2 \alpha = \frac{\frac{1}{r}}{\frac{r}{r}} = \frac{1}{r}$$

$$S = \frac{1}{2} ab \sin \alpha \rightarrow \frac{1}{2} \times \sqrt{r} \times \sqrt{r} \times \sin \alpha = \frac{r}{2} \omega \rightarrow \sqrt{r} \times \sin \alpha = \frac{r}{2} \omega$$

$$\sin \alpha = \frac{\frac{r}{2} \omega}{\frac{\sqrt{r}}{1}} = \frac{\sqrt{r}}{2} \rightarrow \alpha = 30^\circ \text{ to } 150^\circ \quad \frac{r \omega}{2} = r$$

$$\frac{a}{b} = \frac{r}{r} \quad S = ab \sin \alpha = \omega r \rightarrow (rk)(rk) \left(\frac{1}{2}\right) = \omega r \rightarrow rk^2 = \omega r \rightarrow k = \sqrt{\omega}$$

$$a = r(\sqrt{r}) = 9\sqrt{r}, b = r(\sqrt{r}) = 9\sqrt{r} \rightarrow \frac{a+b}{2} = r(a+b) = r(9\sqrt{r} + 9\sqrt{r}) = 18\sqrt{r}$$

$$S_{ABC} - S_{ADE} = 1, \sqrt{6}$$

$$\left(\frac{1}{2} \times \omega \times \sqrt{r} \sin \alpha\right) - \left(\frac{1}{2} \times r \times \sqrt{r} \sin \alpha\right) = 1, \sqrt{6} \rightarrow \frac{r \omega}{2} \sin \alpha - \frac{r^2}{2} \sin \alpha = 1, \sqrt{6}$$

$$\sin \alpha = \frac{1, \sqrt{6}}{\frac{r \omega}{2}} = \frac{1}{r} \quad \cos \alpha = \frac{\sqrt{r}}{r} \rightarrow \alpha = 30^\circ \quad \tan \alpha = \frac{\frac{1}{r}}{\frac{\sqrt{r}}{r}} = \frac{1}{\sqrt{r}}$$

$$S_{ABC} = \frac{1}{2} \times \overline{AB} \times \overline{BC} \times \sin B = r \left(\frac{1}{2} \times \overline{BM} \times \overline{BN} \times \sin B \right)$$

$$(\overline{AB} \times \overline{BC}) = r \times \overline{BM} \times \overline{BN} \rightarrow (\overline{AM} + \overline{BM})(\overline{BN} + \overline{NC}) = r(\overline{BM} \times \overline{BN})$$

$$\frac{\omega}{r} \overline{BN} (\overline{AM} + \overline{BM}) = r \times \overline{BM} \times \overline{BN} \rightarrow \frac{\omega}{r} (\overline{AM} + \overline{BM}) = r \overline{BM} \rightarrow \left(\frac{\omega}{r} \overline{AM} = \frac{r}{r} \overline{BM}\right)$$

$$\omega \overline{AM} = r \overline{BM} \rightarrow \overline{BM} = \frac{\omega}{r} \overline{AM} \quad \left(\frac{BM}{AM} = \frac{\omega}{r} \right)$$

$$\frac{1}{\sqrt{\cos \alpha}} \rightarrow \tan \alpha = \frac{1 \sin \alpha}{1 \cos \alpha} = \frac{1 \sin \alpha}{\cos \alpha} = \left(-\frac{1}{\cot \alpha}\right) \rightarrow |\sin \alpha| = -\sin \alpha \rightarrow \sin \alpha < 0$$

$$\frac{1}{|\cos \alpha|} = \frac{\sin \alpha}{\cos \alpha} = \frac{1 - \sin \alpha}{\cos \alpha} \quad \text{if } \cos > 0 \quad \frac{-\sin \alpha}{\cos \alpha}$$

$$\frac{1 - \sin \alpha}{\cos \alpha} \rightarrow \frac{1 + \sin \alpha}{\cos \alpha} \quad 1 - \sin \alpha = 1 + \sin \alpha \rightarrow \sin \alpha = 0 \rightarrow \sin < 0 \quad \times$$

$$\text{if } \cos < 0 \rightarrow \frac{1}{-\cos \alpha} + \frac{\sin \alpha}{-\cos \alpha} = \frac{1 + \sin \alpha}{-\cos \alpha} \rightarrow \frac{1 + \sin \alpha}{-\cos \alpha} = \frac{1 + \sin \alpha}{r \cos \alpha} \rightarrow \cos \alpha < 0 \quad \checkmark$$

$$\sin < 0 \rightarrow \cos < 0 \rightarrow \left(\frac{r}{r}\right)$$