

الف) $a_1 = 2$ $a_2 = 11$ $a_3 = 24$ $a_4 = 45$ $a_5 = 74$

$2, 11, 24, 45, 74, \dots$

ب) $a_1 = \frac{1}{2}$ $a_2 = \frac{2}{9}$ $a_3 = 1$ $a_4 = \frac{9}{16}$ $a_5 = \frac{16}{25}$

$\frac{1}{2}, \frac{2}{9}, 1, \frac{9}{16}, \frac{16}{25}, \dots$

الف) $t_{13} = \frac{(-1)^{13}}{\sqrt{13+2}} = \frac{-1}{\sqrt{15}} = -\frac{1}{\sqrt{15}}$

۲

ب) $t_{13} = 29 - \left[\frac{13}{2} \right] = 29 - 6 = 23$

الف) $2n < 10$ $n < 5$ $\frac{5}{-2}$ $\{1, 2, 3, 4\}$ $n \in \mathbb{Z}$

۳

ب) $n^2 - 14n + 49 \geq (n-7)(n-7) \leq 0$ $\frac{7}{-1}$ $\{7, 10\}$ $\{2, 4, 6, 8, 10\}$ $n \in \mathbb{Z}$

الف) $2n - 14 \leq 0$ $2n \leq 14$ $n \leq 7$ $\frac{7}{-2}$ $\{1, 2, 3, 4, 5, 6, 7\}$ $n \in \mathbb{Z}$

۴

ب) $n^2 - 12n + 36 \leq 0 \Rightarrow (n-6)(n-6) \leq 0$ $\frac{6}{-1}$ $[6, 6]$ $\{3, 4, 5, 6, 7, 8, 9\}$ $n \in \mathbb{Z}$

$\begin{cases} a_2 = 2a + d = 11 \\ a_3 = 3a + d = 24 \end{cases} \Rightarrow \begin{cases} 2a + d = 11 \\ 3a + d = 24 \end{cases} \Rightarrow \begin{cases} 2a + d = 11 \\ a + d = 13 \end{cases} \Rightarrow \begin{cases} a = -2 \\ d = 15 \end{cases}$

۵

$t_2 = 1a + d = 9 - 2 = 7$

الف) $x_{\min} \xrightarrow{a>0} n = \frac{-b}{2a} = \frac{-4}{2} = -2$

$y_{\min} = \frac{9-16+2}{-2} = -\frac{5}{2}$

۶

ب) $x_{\min} \xrightarrow{a>0} n = \frac{-b}{2a} = \frac{-4}{2} = -2$

$y_{\min} = \frac{-4-16+1}{-2} = -\frac{19}{2}$

این متن به زبان فارسی است $\rightarrow$ ن باید حداقل باشد

① $-4, -1, 2, 5, 8, \dots$ $a_1 = -4$ $a_2 = -1$ $a_3 = 2$ $a_4 = 5$ $a_5 = 8$

$a_1 = -4$ $a_2 = -1$ $a_3 = 2$ $a_4 = 5$ $a_5 = 8$

$an^2 + bn + c \xrightarrow{\text{مقایسه}} n^2 - 4n + 1$

$t_1 = -4 = 1 + 1 + b \rightarrow b = -4$

۷

$t_1 = 1 - 4 + 1 = -2$

$t_1 = 1(1)^2 + b - 4 = -4 \rightarrow b = -1$

۸

$n^2 - n - 4$

$a+4 \leq 2a+1$ $4-1 \leq 2a-a$ $a \geq 3$ $[3, +\infty)$

۹

الف) $\left[\frac{1}{2} \right] = 2$

۱۰

ب) $\left[\frac{1}{2} \right] = 2$

ج) $\left[\frac{1}{15} \right] = 4$

د) $n(A \cup B) = n(A) + n(B) - n(A \cap B) = 13 + 12 - 4 = 21$